

1 **Effect of Subgrade on Tensile Strains in a Geomembrane for**
2 **Tailings Storage Applications**

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14 **Abstract:** Experiments are conducted to quantify short-term tensile strains induced in
15 a 1.5-mm-thick high-density polyethylene geomembrane overlain by tailings. Four
16 subgrades, a poorly graded angular to sub-angular gravel (GP), a well-graded angular
17 to sub-angular gravel (GW), a poorly subrounded graded sand (SP), and silty sand (SM),
18 and two nonwoven geotextiles, 450 g/m² and 1420 g/m², are evaluated. All the
19 indentations in the geomembrane are due to the subgrade, and with an adequate fraction
20 of sand size particles in the subgrade, the tensile strains can be minimized. At 2000 kPa,
21 the maximum tensile strain is 32% for GP, 16% for GW, 13% for SP, and no discernable
22 indentation is observed for SM prepared at the optimum water content of 11%. For the
23 soft SM subgrade prepared at 20% water content, only one indentation with the tensile
24 strain of 2% is observed. At 2000 kPa, a 450 g/m² geotextile beneath the GMB reduces
25 the maximum tensile strain from 32% to 23% for GP subgrade, from 16% to 8% for
26 GW subgrade, and from 13% to 6% for SP subgrade; the 1420 g/m² geotextile reduces
27 the maximum tensile strain to 14% for GP subgrade. Thus, minimal subgrade
28 indentation induced strain and hence the possibility of a very long service life of
29 geomembrane can be achieved using SM subgrade.

30

31 **Keywords:** Geosynthetics, Geomembrane, Geotextile, Tailings, Geomembrane Strain

32

33 **1. Introduction**

34 Tailings storage facilities (TSFs) are engineered structures constructed to impound
35 slurry, thickened, and paste tailings resulting from mineral processing activities. With
36 the increase in the footprint of mining sites and the height of tailing dams,
37 geomembranes (GMBs) are increasingly playing a vital role in the containment and
38 erosion control of these facilities (Davies et al. 2002; Thiel and Smith 2004; Touze et
39 al. 2008; Touze 2020; Rowe 2020).

40 The GMB in mining applications is usually either high-density polyethylene
41 (HDPE) or linear low-density polyethylene (LLDPE) with a typical thickness of 1.0 to
42 2.5 mm (Touze et al. 2008; Rowe et al. 2013). To the extent that these GMBs have been
43 used in TSFs, it has most commonly been either as a liner to the tailings dam wall
44 (Giroud 2016; McLeod 2016) or a GMB liner placed on the base in order to reduce the
45 contaminant migration, leakage, and the hydraulic gradient from the facilities to the
46 surrounding environment, and decrease the phreatic surface within the embankment
47 dam to achieve adequate geotechnical stability against failure (Lupo and Morrison 2007;
48 Touze et al. 2008; Rowe et al. 2017; Chou et al. 2018; Rowe 2020; Fan and Rowe 2022a,
49 2022b; Rowe and Fan 2021, 2022). GMB liner systems for TSFs commonly comprise
50 a single GMB liner even though the hydraulic head within the facility can exceed 100
51 m (Touze et al. 2008). This is because tailings with a typical fines content ($<75 \mu\text{m}$) of
52 40-70% can form a lower permeability layer at the base of TSFs above the liner. With
53 these GMBs, the leakage is effectively limited to flow through holes in the GMB that

54 most arise either from short-term puncture (e.g., during construction including
55 placement of materials over the GMB) or subsequently due to long-term stress cracking
56 (Giroud and Bonaparte 1989a, 1989b; Giroud 1997; Peggs et al. 2005, 2014; Rowe
57 1998, 2005, 2012, 2020; Rowe and Yu 2019; Abdelaal et al. 2014; Ewais et al., 2014).

58 Given the large size and remote location of TSFs, the subgrade soil beneath the
59 GMB is often the in-situ or recompacted soil or rock. Therefore, the GMB may be
60 subject to indentations that induce tensile strain from this subgrade. Current practice to
61 assess the performance of GMB with proposed materials overlying and underlying is
62 to conduct short-term cylinder test for 24-100 h to examine whether the GMB punctures
63 (Thiel and Smith 2004; Lupo and Morrison 2007; Brachman et al. 2014). While it is
64 necessary to avoid short-term puncture, the absence of puncture does not mean that
65 holes will not develop with time in areas where there are high tensile strains due to
66 stress cracking. Indentations may arise from stones in the subgrade below the GMB
67 (Brachman and Sabir 2010) or a drainage layer below waste, crushed ore, or tailings
68 (e.g., Rowe et al. 2013; Brachman et al. 2014; Marcotte and Fleming 2019, 2020; Rowe
69 and Yu 2019; Rowe 2020). These indentations induced tensile strain have been shown
70 to cause stress cracking at strains as low as 5% (Abdelaal et al. 2014; Ewais et al. 2014).
71 Thus, there may also be a need to limit the local tensile strains in the GMB that develop
72 at indentations from overlying or underlying materials to ensure adequate long-term
73 performance (Seeger and Müller 2003; Hornsey and Wishaw 2012; Eldesouky and
74 Brachman 2020). Although much is known about local tensile strains that may develop

75 in a municipal solid waste landfill and heap leach applications primarily from gravel
76 above the liner (Tognon et al. 2000; Brachman and Gudina 2008; Rowe et al. 2013;
77 Brachman et al. 2014; Marcotte and Fleming 2019, 2020; Adesokan et al. 2021), there
78 is a paucity of data on the tensile strains that may develop from the subgrade below the
79 GMB in tailings storage facilities.

80 The magnitude of allowable tensile strains that a GMB can sustain without
81 compromising their intended long-term performance reported in the literature varies
82 (Seeger and Müller 2003; Peggs et al. 2005; Rowe et al. 2019b). For example, to avoid
83 premature GMB failure due to stress cracking, Seeger and Müller (2003) recommended
84 that the GMB strain should be less than 3%. Coming from a different perspective, Rowe
85 et al. (2019b) suggested 3-5% depending on the location of the GMB (i.e., 3% on the
86 base, 4% on side slopes, 5% on in the cover). Based on the GMBs examined under the
87 simulated field conditions, it can be inferred that the tensile strains due to a granular
88 drainage layer in a leachate collections system, below ore in a heap leach pad, or below
89 tailings to accelerate consolidation of the tailings can generally be minimized/avoided
90 by using of a suitable protection layer between the GMB and the overlying (Tognon et
91 al. 2000; Brachman and Gudina 2008; Hornsey and Wishaw 2012; Brachman and Sabir
92 2013; Rowe et al. 2013; Abdelaal et al. 2014; Ewais et al., 2014; Marcotte and Fleming
93 2020). It follows logically that for a tailing storage facility, a suitable protection layer
94 below the GMB would also provide protection from indentation induced strains caused
95 by gravel in the subgrade.

96 Nonwoven needle-punched geotextiles (GTXs) are commonly used as a
97 protection/filtration layer between GMB and its underlying/overlying coarse gravels
98 because they are commercially available, easy to install, and economical relative to
99 many of the other options (Rowe 1988, 2005, 2012; Giroud 2016; Lupo 2010; Cazzuffi
100 and Gioffrè 2020). In the tailings storage application where the consolidated tailings
101 have a much lower hydraulic conductivity than natural subgrade materials beneath the
102 GMB, piping is prone to occur when the subgrade soil is filter incompatible with its
103 overlying tailings (Rowe et al. 2017; Chou et al. 2018; Fan and Rowe 2022b). The
104 migration of tailings and the potential piping through any GMB defects can be
105 effectively prevented by introducing a GTX filtration layer that satisfies the retention
106 criterion either above or beneath the GMB (Rowe et al. 2017; Fan and Rowe 2022b).
107 Besides the filtration effect of GTXs, the protection between the GMB and coarse
108 gravels offered by GTXs may comprise two forms. First, as the gravel particle deforms
109 into the GTX, the thickness of the GTX is reduced, and the contact area between gravel
110 particle and GTX increases. This spreads the gravel force over a larger area, resulting
111 in a slightly wider indentation and thereby smaller strains in the GMB relative to no
112 protection. This is commonly referred to as cushioning (Brachman and Sabir 2013).
113 Second, as the GTX deforms, membrane tensions can be mobilized in the GTX, further
114 reducing the contact force applied to the GMB from the gravel particle (Brachman and
115 Sabir 2013). The amount of membrane tension mobilized depends on the slack in, and
116 stiffness of, the GTX together with the magnitude of displacement. Although the

117 filtration effect of GTX was proven to effectively prevent piping through any existing
118 GMB holes in TSFs (Rowe et al. 2017; Fan and Rowe 2022b), and the satisfactory
119 protection effect of GTX in minimizing tensile strains of a GMB in municipal solid
120 waste landfills (Rowe 2005, 2012, 2020; Brachman and Gudina 2008; Brachman and
121 Sabir 2013; Eldesouky and Brachman 2020) and in water impoundments (Giroud 2016;
122 Lupo 2010; Cazzuffi and Gioffrè 2020), the effectiveness and suitability of a GTX as
123 a protection layer in minimizing tensile strains of a GMB for a tailings storage
124 application is unknown.

125 Thus, the objective of this paper is to quantify the short-term tensile strains
126 induced in a 1.5-mm-thick HDPE GMB from different: (1) subgrades, (2) consolidation
127 stresses, and (3) geotextile protection layers.

128 **2. Experimental Investigation**

129 ***2.1 Test Apparatus and Method***

130 A cylindrical steel pressure vessel with an inside diameter of 590 mm and a height of
131 500 mm (Fig. 1) was used to examine the response of a GMB to different subgrade
132 materials. Vertical pressures (σ_v) of 500 kPa, 1000 kPa, and 2000 kPa were applied by
133 hydraulic pressure injected between the steel and the rubber bladder shown in Fig. 1.
134 The steel pressure vessels had a capacity of 3000 kPa. Horizontal pressures
135 corresponding to conditions of zero lateral strain were developed by limiting the
136 outward deflection of the thick walled steel test apparatus. A friction treatment was
137 used to reduce side wall friction along the vertical boundaries of the test apparatus to

138 less than 5% (Tognon et al. 1999; Brachman et al. 2014).

139 **2.2 Geomembrane**

140 A smooth HDPE GMB with a thickness of 1.5 mm was examined. This type and
141 thickness of GMB was one of the most commonly used in recent mining application
142 worldwide (Rowe et al. 2013), presumably because its high strength and excellent
143 chemical resistance to a wide range of chemicals due mainly to its high crystallinity (40%
144 - 60%). The density of the GMB examined was 947 kg/m³. Additional index tensile
145 properties of the GMB are given in Table 1. All the GMB tested were obtained from
146 the same roll.

147 **2.3 Tailings**

148 The tailings examined, from a mining facility in British Columbia (Canada), was silty
149 sand (denoted as SM in the USCS classification) with 30% nonplastic fines (<75 µm;
150 Table 2 and Fig. 2) and a specific gravity of ~2.65. Based on consolidation tests, the
151 voids ratio – effective stress relationship was given by (Fan and Rowe 2022a; Fan et al.
152 2022):

$$153 \quad e = -0.046 \ln \sigma'_v + 0.755 \quad (1)$$

154 **2.4 Subgrades**

155 Four subgrades were studied (detail properties are given in Table 2 and Fig. 2):

- 156 1. a poorly graded angular to sub-angular gravel (GP) with a uniformity coefficient,
157 $C_u \sim 4$,
- 158 2. a well-graded graded angular to sub-angular gravel (GW),

159 3. a poorly graded subrounded sand (SP) also with $C_u \sim 4$,

160 4. a silty sand (SM) with 18% nonplastic fines.

161 The GW subgrade was more well-graded than the GP gravel and the gradation curve
162 converged with GP for particle sizes larger than 6.7 mm. 24% of the GW subgrade was
163 < 6.7 mm and had a minimum grain size (0.6 mm; retained on No. 30 sieve) very close
164 to that for the SP subgrade (0.43 mm; retained on No. 40 sieve). The subgrade materials
165 for GP, GW, and SP were comprised of angular to sub-angular particles arising from
166 crushing stone for particle size larger than 1.18 mm (No. 16 sieve) and sub-angular
167 silica sand for particle size smaller than 1.18 mm (see Fig. 3). As placed, the GP, GW,
168 and SP subgrades were relatively incompressible compared to the compressible, loosely
169 placed, silty sand tailings which experienced about 100 mm of settlement with the
170 increase in stress to 2000 kPa. There was no discernable settlement for GP, GW, and
171 SP subgrades after consolidated at 2000 kPa for around 100 hours. The SM subgrade
172 was cyclone silty sand tailings sourced from the same mining facility as the overlying
173 tailings (Fig. 2 and Table 2).

174 **2.5 Geotextiles**

175 Two nonwoven needle-punched geotextiles, denoted as GTX1 and GTX2 (Table 3)
176 were used as a single protection layer between GMB and the subgrade materials. GTX1
177 was a needle-punched nonwoven with a random network of 100% virgin polypropylene
178 staple fibers and a mass per unit area, $M_a = 450$ g/m². GTX2 was a needle-punched
179 staple fiber nonwoven product manufactured using blends of polypropylene and

180 polyester resins with $M_a = 1420 \text{ g/m}^2$. The apparent opening size (AOS) was 0.15 mm
181 for GTX1 and 0.075 mm for GTX2. Based on the comparison between the particle size
182 of silty sand and the AOS of geotextile, the geotextile satisfied the retention criteria
183 summarized by Gardoni and Palmeira (2002). The two GTXs examined are widely
184 used as the protection layer in the North America. Although much heavier protection
185 GTX is recommended in some regions (e.g., Germany), it is very rarely used in mining
186 application due to cost which exceeds that of the geomembrane, and so this study is
187 directed to illustrating the feasibility of GTX examined herein to reduce tensile strains
188 arising from the subgrades of interest.

189 **2.6 Test Procedure**

190 The 200-mm-thick subgrade was placed in several lifts, with care being taken to avoid
191 segregation during placement. Each lift was tamped using a steel block to produce as
192 flat a surface as possible. The dry density of the GP, GW, and SP subgrades varied
193 between 1700 and 1900 kg/m^3 .

194 Test 8 was conducted to investigate the effect of subgrade stiffness on the GMB
195 indentation and stains (Table 4). In this case, the silty sand subgrade (SM) was
196 compacted in seven 30-mm-thick lifts with a steel block to a density of 2000 kg/m^3 at
197 ~20 % gravimetric water content, which was notably higher than its Standard Proctor
198 optimum moisture content of 11%. This was to simulate the scenario where the cyclone
199 silty sand tailings were used as the subgrade earthwork construction materials for a TSF.
200 For Test 9, the silty sand subgrade (SM) was compacted at the Standard Proctor

201 optimum moisture content of ~11% following the same procedure as that for Test 8.

202 To study its impact on the GMB local indentation and the resultant tensile strain,
203 some tests were conducted without a GTX protection layer, some with a layer of GTX1
204 and some with a layer of GTX2 between the subgrade and the GMB (Table 4, Fig. 1).
205 To permanently preserve the deformation of the GMB after removal of the load, two
206 rectangular soft lead sheets, 160 mm wide \times 270 mm long each and 0.4-mm-thick, were
207 placed on the upper surface of the GMB. The lead sheet was sufficiently thin and soft
208 so that it did not locally stiffen the response of the GMB as previously demonstrated
209 by several investigators (e.g., Tognon et al. 2000; Brachman and Gudina 2008).

210 For the tests with GP, GW, and SP subgrades, fully saturated silty sand tailings
211 slurry with approximately 70% solids content was placed above the GMB to a thickness
212 of approximately 300 mm. To prevent any preferential flow around the circumference
213 of the GMB, a bentonite perimeter seal was introduced around the top and bottom of
214 the GMB edges. After 24 hours deposition and settlement of the slurry, a sand leveling
215 layer, wrapped in a separator geotextile, was used to fill the gap between the top of
216 tailings and the rubber bladder. The final thickness of tailings after the consolidation
217 was close to 200 mm. For Tests 8 and 9 in Table 4 with SM subgrade, the overliner
218 tailings was prepared using the same procedure as the SM subgrade at the water content
219 of 12% until reaching a final thickness of 200 mm.

220 At the start of a test, pressure was applied at a rate of 10 kPa per minute until the
221 target pressure σ_v of 500, 1000, or 2000 kPa was reached (see Table 4). For the tests

222 with GP, GW, and SP subgrades, tailings were consolidated at 250, 500, and 1000 kPa
223 for σ_v of 500, 1000, and 2000 kPa, respectively, by maintaining the pore pressure u of
224 250, 500, and 1000 kPa, respectively, within the tailings through two drainage ports at
225 the sidewall of the cell (Fig. 1). Adopting a unit weight of water is 9.8 kN/m^3 and the
226 submerged unit weight of tailings of 10 kN/m^3 , the simulated tailings thickness, denoted
227 as T , and the water head above the GMB, denoted as H , were 25 m and 25.5 m,
228 respectively, for $\sigma_v = 500 \text{ kPa}$ and $u = 250 \text{ kPa}$, 50 m and 51 m, respectively, for $\sigma_v =$
229 1000 kPa and $u = 500 \text{ kPa}$, and 100 m and 102 m, respectively, for $\sigma_v = 2000 \text{ kPa}$ and
230 $u = 1000 \text{ kPa}$.

231 The pressure applied on the GMB, σ_v , was unaffected by the consolidation of
232 tailings since this it was externally applied. However, the stiffness of tailings in contact
233 with the GMB progressively increased with increasing effective stress and this may
234 affect the tensile strains induced in the GMB. The target pressure was held constant for
235 around 100 h. The consolidation of tailings was accelerated by periodically opening the
236 two drainage ports on the sidewall of the cell (Fig. 1). After reaching the target σ_v and
237 u within the cell, 100% consolidation of tailings was reached when pore pressure, u ,
238 monitored by pressure transducer did not increase with the closing the sidewall drainage
239 ports, (i.e., no excess pore water migration towards the drainage ports). The 100 h test
240 duration chosen herein was notably greater than the 24 hours required for the
241 consolidation of tailings and hence considered to be adequate to acquire the
242 indentations. These strains represent most of the strains likely to be developed, however,

243 it is acknowledged that there may be further strain increases with additional time due
244 to long-term time-dependant deformation of the subgrade. All the experiments were
245 conducted at a temperature of 21 ± 2 °C; as such, the strains may underestimate the
246 pressures if service temperatures are higher.

247 After the completion of a test, the test cell was depressurized and the tailings
248 removed to allow examination of the GMB and the lead sheets. After carefully
249 removing the GMB and lead sheets from the cell, each GMB sample was examined
250 visually for scratches, signs of yielding, and notable indentations. The GMB was
251 visually checked for puncture with back-light in a dark room. A mould of the lead sheet
252 was cast with low-shrinkage plaster of Paris to permanently preserve its deformed shape.
253 The major indentations in the lead sheets were identified and the surface was scanned
254 using a laser scanner to quantify indentations and hence allow the evaluation of the
255 strains using the method of Tognon et al. (2000). Since the post-test indentations were
256 all from the subgrade materials (as discussed later), there was an observation error
257 arising from the thickness of lead sheet above the GMB. The real profile of indentation
258 on the GMB surface was actually widened by the scanned indentation on the upper
259 surface of lead sheet, which slightly underestimated the real tensile strain. As shown by
260 Brachman and Gudina (2008), the small underestimate in tensile strain due to the lead
261 sheet thickness could be neglected for the 0.4-mm-thick lead sheet used.

262 **3. Results: GMB Tensile Strains**

263 The GMB was not punctured in any of these short-term tests; however, significant
264 tensile strains were mobilized in the GMB for some tests. For the tests with GP, GW,
265 and SP subgrades, all the indentations were from the bottom of the GMB and hence
266 were attributed to the subgrade. This is because these subgrades were much stiffer and
267 coarser than the overlying tailings. The GMB tensile strain evaluated using the method
268 of Tognon et al. (2000) considers both the membrane and the bending components of
269 strain. While membrane strain is uniform throughout the thickness of the GMB,
270 bending strain varies from zero at the middle surface of the GMB to being greatest at
271 the extreme fibers (where stress cracking will be initiated). Strains for the subgrades of
272 GP, GW, and SP were calculated for at least 13 of the most prominent indentations in
273 two lead sheets for each test. For Test 8 with SM subgrade compacted at ~20%
274 gravimetric water content, there was only one discernable indentation that could be
275 analyzed; whereas for Test 9 with SM subgrade compacted at the Standard Proctor
276 optimum moisture content of ~11%, no discernable indentation was observed (Fig. 4).
277 The largest three tensile strains from each test are given in Table 4.

278 **3.1 Effect of Subgrade**

279 The seven largest strains calculated from the tests with GP, GW, and SP subgrades are
280 shown in Fig. 5. Subgrade GP was the coarsest examined, leading to the most prominent
281 local tensile strains at the same applied pressure. For example, the maximum tensile
282 strain at 2000 kPa was 32% for GP subgrade, 16% for GW subgrade, 13% for SP
283 subgrade, and ~ 0% for SM subgrade compacted at optimum water content (Table 4).

284 Subgrade GW contained more finer component (< 6.7 mm) than GP, these finer
285 particles fit in around the larger particles reduced local irregularities in GMB settlement
286 and local indentations in the GMB (see Figs. 6a and 6b). Consequently, the seven
287 largest GMB tensile strains for GW were reduced by an average factor of 1.7 at 2000
288 kPa, 1.4 at 1000 kPa, and 1.8 at 500 kPa relative to GP, but all cases exceeded a
289 maximum desirable tensile strain from all sources of 5% (Rowe et al. 2019b).

290 Subgrade SP was the finest examined among GP, GW, and SP subgrades. With
291 the same shaped gradation curve as GP, subgrade SP had smaller maximum and
292 minimum grain sizes (Fig. 2), the resultant seven largest GMB tensile strains for SP
293 were reduced by a factor of 2.6 at 2000 kPa relative to GP (Fig. 5c). Subgrade GW was
294 more well-graded than SP and had a very close minimum grain size (0.6 mm) to that of
295 SP (0.43 mm). However, because of a much larger maximum grain size for GW (63.5
296 mm) than for SP (9.5 mm) and the consequent greater surface irregularities, the
297 resultant seven largest GMB tensile strains for subgrade GW at 2000 kPa was in
298 average 1.6-fold higher than those for subgrade SP.

299 Therefore, both the maximum and the minimum subgrade grain sizes affected the
300 local indentations and tensile strains in GMB. Since the subgrade particles were much
301 stiffer than tailings, the particles at the subgrade surface might locally attract force due
302 to the uneven surface arising from the surface irregularity (see Figs. 6a and 6b),
303 resulting in local irregularities in GMB settlement and local indentations in the GMB
304 that may lead to tensile strains. Decreasing the maximum grain size and increasing the

305 finer portion (sand size particles) to fill the gap between the adjacent coarse particles
306 both improved the surface irregularity and reduced the GMB tensile strains.

307 **3.2 Soft Subgrade**

308 The high initial water content (~20%) in Test 8 exploring the scenario of using the
309 cyclone silty sand tailings as the subgrade earthwork construction materials produced
310 a SM subgrade with low stiffness and high compressibility, compared with the lower
311 initial water content (~12%) overlying tailings. During the test, excess pore water
312 within the subgrade was allowed to seep through the outlet drain at the bottom of the
313 steel vessel. Post-test exhumation revealed that there had been some consolidation of
314 the subgrade and the final water content was ~15%. No distinct indentation was
315 observed visually at 500 kPa, showing the negligible impact arising from the
316 differential stiffness between the subgrade and the overliner. Only one indentation with
317 the tensile strain of 2% was detected by the laser scanner. The indentation was likely
318 due to the differential settlement (<1 mm) resulting from minor differences in density
319 of the subgrade. Brachman et al. (2014) experimentally examined the local tensile
320 strains within a 1.5-mm-thick HDPE GMB in heap leach applications. There was a 150-
321 mm-thick silty sand layer, compacted to its Standard Proctor maximum dry density,
322 underlying and overlying the GMB as the subgrade and the protection layer,
323 respectively. The largest tensile strain was no greater than 2% at the vertical pressure
324 of 3000 kPa. Summarizing the findings of Tests 8 and 9 and Brachman et al. (2014),
325 the SM subgrade was very effective at reducing local indentations in the GMB, even

326 when it was compacted at a water content notably higher than its optimum water content.

327 **3.3 Effect of Geotextile Protection Layer**

328 Due to the cushioning effect arising from the GTX, each GMB indentation was widened
329 (see Fig. 6c), reducing the steepness of deformation and tensile strain. The seven largest
330 strains calculated from the tests with GTX protection layer at 2000 kPa are shown in
331 Fig. 7. For the 450 g/m² GTX1, the maximum tensile strain at 2000 kPa reduced from
332 32% to 23% for GP, 16% to 8% for GW, and 13% to 6% for SP; the seven largest GMB
333 tensile strains at 2000 kPa were reduced by a factor of 1.4 for GP subgrade (Fig. 7a),
334 2.2 for GW subgrade (Fig. 7b), and 2.3 for SP subgrade (Fig. 7c), compared with the
335 corresponding tests without GTX protection. Meanwhile, for the tests with GP subgrade,
336 increasing the pressure from 500 kPa to 1000 kPa, and finally to 2000 kPa, the
337 maximum tensile strain with the 450 g/m² GTX1 protection decreased from 14% to 7%
338 at 500 kPa, 17% to 10% at 1000 kPa, and 32% to 23% at 2000 kPa, the seven largest
339 GMB tensile strains were reduced by a factor of 2.2, 1.6, and 1.4, respectively,
340 reflecting the decreasing GTX cushioning effect with the increasing pressure.

341 Brachman and Gudina (2008) classified contact types between 1.5-mm-thick HDPE
342 GMB and two poorly graded angular gravels into point, edge, area, perimeter, and
343 composite contacts. For two angular gravel subgrades evaluated by Brachman and
344 Gudina (2008), approximately 40% of the contacts were point contacts, the steepest
345 GMB indentations and the largest tensile strains were caused by point and edge contacts.
346 The GTX thickness became smaller with the increasing pressure, point and edge

347 contacts both locally attracted more force than the others contact types, leading to a
348 further reduction in both the GTX thickness and cushioning effect. Therefore, the
349 reduction factor arising from the GTX1 protection layer for the seven largest GMB
350 tensile strains decreased with the increasing pressure.

351 For Test 3B with the 1420 g/m² GTX2 as protection layer, the seven largest GMB
352 tensile strains at 2000 kPa (Fig. 7a) were reduced by a factor of 2.4 compared with
353 those for Test 3 without protection layer, and the maximum strain decreased from 32%
354 to 14%. The strains for Test 3B (GTX2) were notably less than those for Test 3A (GTX1)
355 with the maximum strain of 23% for Test 3A and 14% for Test 3B. This is because with
356 the increasing GTX mass from 450 (GTX1) to 1420 g/m² (GTX2), a greater cushioning
357 effect was provided and hence the indentations became wider; also, as the stiffness of
358 the protection layer increased, more membrane tensions were mobilized in the GTX2.
359 Consequently, the protection layer took greater force, less force was transferred to the
360 GMB and the subgrade, resulting in smaller indentations and tensile strains for Test 3B.
361 The seven largest GMB tensile strains at 2000 kPa were very similar between the
362 subgrades of GP + GTX2 and SP (Figs. 7a and 7c), representing the efficacy of
363 geotextile relating to minimizing the tensile strains in a GMB.

364 Fine tailings consolidate slowly, on the order of decades, resulting in a much
365 greater piping potential through the unconsolidated or partially consolidated tailings in
366 the short term than through the consolidated tailings in the long term. A GTX protection
367 /filtration /separation layer is a practical way of preventing piping at the early stage of

368 a TSF where a filter compatible subgrade is not easy to be achieved. Since this is a
369 temporary need for the GTX, a GTX selected to have adequate filtration characteristics
370 and service life, may be appropriate. However, if the GTX layer is introduced above
371 the GMB, the lateral interface transmissivity of GTX more readily transmits flow to the
372 GMB hole from further away than when the tailings are in direct contact with the GMB,
373 resulting in a 60% increase in the measured leakage through a 10-mm-diameter hole
374 (Rowe et al. 2017). Furthermore, introducing the GTX above the GMB has no
375 significant impact on the GMB indentations and tensile strains since the indentations
376 primarily arise from the bottom of the GMB due to the higher stiffness of the subgrade
377 than the overlying tailings. In contrast, introducing the GTX beneath the GMB slightly
378 decreased leakage through a 50-mm-diameter hole by up to 15% relative to the case
379 without the GTX protection layer (Fan and Rowe 2022b), and notably reduced the
380 GMB tensile strains (Figs. 6c and 7), especially for the GW and SP subgrades, or a
381 thicker GTX. The decrease in leakage may be caused by the clogging of GTX by
382 particles passing through the hole. With a GTX protection layer below the GMB, the
383 leakage through a larger hole was still notably greater than that through a smaller hole,
384 which highlights the importance of avoiding large localized GMB tensile strain to
385 minimize the potential leakage in the long term (the effect of hole size on leakage can
386 be assessed for a circular hole from Fan and Rowe (2022a) and for the more general
387 case of circle, rectangle, or slit from Rowe and Fan (2022)). Thus, if a GTX
388 filter/separator/protector layer is to be used in the tailings storage applications for

389 minimizing the risk of piping and reducing the GMB tensile strain, it should be between
390 the GMB and the subgrade and not between the tailings and GMB.

391 **3.4 Effect of Applied Pressure**

392 The influence of pressure on GMB strain using GP and GW subgrades is shown in Fig.
393 8. There is an overall trend of the three largest values of strains from each test series
394 increasing with the applied pressure since narrower and deeper indentations arose from
395 larger pressures. There is a poor correlation between the pressure and both the three
396 largest strains and the maximum strain. This is considered to be caused by the
397 variability of the subgrade surface irregularity among different tests for the same type
398 of subgrade, creating different distributions of localized point and edge contacts on the
399 GMB. Due to the GTX cushioning effect and the higher finer component within GW
400 subgrade, the maximum strains for both the GP subgrade with GTX1 and the GW
401 subgrade without GTX were below the maximum strain for GP subgrade at each
402 applied pressure (Fig. 8).

403 Based on the data available, the relationship between the average three largest
404 tensile strains (%) and applied stress σ_v (kPa; $500 \text{ kPa} \leq \sigma_v \leq 2000 \text{ kPa}$) can be
405 approximately correlated as follows:

$$406 \quad \textit{strain for GP} = 0.01\sigma_v + 7 (\%) \quad (2)$$

$$407 \quad \textit{strain for GW} = 0.005\sigma_v + 6 (\%) \quad (3)$$

408 The parameters in Eqs. 2 and 3 are highly dependent on the coarser particle within the
409 subgrade, represented by D_{85} , and the shape of the subgrade gradation curve,

410 represented by C_c . As noted that the stress crack is likely to be induced once the
411 minimum strain exceeds 6%. The length of time until stress cracking occurs will be
412 primarily dependent on the magnitude of the strain (generally speaking, the greater the
413 strain the sooner the stress cracking) and the representative stress crack resistance of
414 the material (Rowe et al. 2019a).

415 **3.5 Repeatability of Test Results**

416 The repeatability of test was examined by conducting a duplicate of Test 3 (denoted
417 Test 3R) at 2000 kPa with the coarsest GP subgrade (Table 4) since this was expected
418 to give the largest variability due to fewer, larger, and more variable particles in this
419 subgrade. The tensile strains for the seven most prominent indentations in (Tests 3 and
420 3R) were (32%, 30%), (29%, 27%), (25%, 26%), (22%, 26%), (22%, 26%), (21%, 24%),
421 and (20%, 24%). Although the maximum tensile strain of 30% for Test 3R was slightly
422 less than 32% for Test 3, the average of both three and seven maximum tensile strains
423 for both tests were close. The difference in the average of the 7 largest strains (24% and
424 26%) was 2% (i.e., 11% of the strain measured). Therefore, the aforementioned
425 conclusions also apply to Test 3R. The number of the indentations/m² with the tensile
426 strain \geq 6% was 670 for Test 3R and was 463 for Test 3, and the number of the
427 indentations per square meter GMB with the tensile strain \geq 12% was 648 for Test 3R
428 and was 394 for Test 3. Thus, more stress cracking is to be expected for the subgrade
429 produced in Test 3R. The particle sizes for the GP examined varied from the smallest
430 value of 3.35 mm to the largest value of 63.5 mm (Figure 2). The orientations of those

431 angular to sub-angular particles may lead to different contact types (e.g., point, edge,
432 area, and perimeter) with the overlying GMB, leading to a notable difference in GMB
433 tensile strains and variation in strain distribution.

434 **4. Practical Implications**

435 There were no punctures due to the subgrade in any of the cases tested and hence
436 negligible leakage in the short-term due to the subgrade, although there may be short
437 term leakage due to other defects (e.g., defective seams). However, eventually stress
438 cracking can be expected at all locations with tensile strains in excess of about 6% (for
439 both HDPE and LLDPE), with it occurring sooner by the larger strain. To quantify the
440 distribution of strains arising from the subgrade conditions, the number of the
441 indentations/m² with the tensile strain $\geq 5\%$ was predicted based on the scanned
442 indentations in the two rectangular lead sheets with the dimension of 160 mm \times 270
443 mm each as summarized in Fig. 9. Table 5 gives the number of tensile strains $\geq 6\%$ for
444 applied pressures of 500, 1000, and 2000 kPa. At 2000 kPa, there were ~ 394 tensile
445 strains exceeding 12% per m² and 463 tensile strains/m² exceeding 6% for GP. There
446 were ~ 128 and ~ 324 tensile strains/m² exceeding 12% and 6%, respectively, for GP +
447 GTX1, while increasing the geotextile thickness reduce that to ~ 23 exceeding 12% and
448 127 exceeding 6% tensile strains/m² for GP+GTX2. For the GW subgrade, there were
449 ~ 197 exceeding 12% and 394 exceeding 6% tensile strains/m², while adding the
450 geotextile (GW + GTX1) reduce this to ~ 139 tensile strains/m² exceeding 6%. For SP
451 there were ~ 15 and 174 tensile strains/m² exceeding 12% and 6%, respectively, and

452 adding GTX1 reduce this to ~ 23 tensile strains/m² exceeding 6% for SP + GTX1,
453 illustrating the effect of the subgrade sand size particle and GTX on reducing the GMB
454 tensile strain.

455 GP + GTX1 outperformed GW regarding the number of indentations with tensile
456 strains $> 6\%$, however, both the number of strains $>15\%$ and the maximum strain for
457 GP + GTX1 were greater than those for GW; whereas GP + GTX2 had a similar strain
458 distribution as SP alone and GW + GTX1 outperformed SP (Fig. 9). Therefore, better
459 protection effect was achieved by using a thicker GTX; however, placing the GTX
460 protection layer beneath the GMB does not guarantee a better performance than
461 increasing the proportion of sand size particle in the subgrade. The effectiveness and
462 capability of GTX should be assessed by conducting a test similar to those described
463 herein for the anticipated subgrade, GTX, GMB and tailings to assess the benefit of the
464 proposed geotextile in a given situation.

465 Every indentation yielding a tensile strain greater than 6% there will eventually
466 be over 10,000 stress cracks per hectare, although the time to stress cracking (service
467 life) will increase with the fewest strains in excess of 6% and the higher the
468 representative stress crack resistance SCR_m of the GMB (Rowe et al. 2019b).

469 The only design scenario examined that is likely to offer a very long service life
470 is to use the SM as the subgrade. The number holes must be considered in the context
471 of the leakage that would occur. Based on stress cracks observed by Ewais et al. (2014),
472 Abdelaal et al. (2014), and Rowe and Fan (2022), three stress crack sizes (i.e., 10 mm

473 $\times 0.5$ mm, 20 mm $\times 1.6$ mm, and 30 mm $\times 3.75$ mm) were considered, with the number
474 of stress cracks predicted per ha for the different subgrades and applied pressures in
475 Table 5. The leakage was calculated using tailings parameters and the model proposed
476 by Rowe and Fan (2022), and neglected the effect arising from the adjacent defects.

477 With SM subgrade, no subgrade induced stress cracking is anticipated and with
478 an appropriate geomembrane a long service life with minimal leakage can be
479 anticipated at all three stress levels examined. Wherever possible, a similar or better
480 subgrade is recommended. However, that will not always be possible.

481 For the GW subgrade at $\sigma_v = 500$ kPa, the calculated leakage ranges between
482 79,000 and 785,000 liters per hectare per day (lphd). To put this into context, based on
483 Beck (2015) less than 5% of composite liners in New York State landfills had leakage
484 exceeding 1,000 lphd, illustrating the inadequacy of GW subgrade as bedding soil for
485 the GMB liner. When the stress is increased to 2000 kPa for the same GW subgrade the
486 leakage increases to between about 790,000 and 7,804,000 lphd. If the nature of the
487 subgrade cannot be readily changed, then the addition of the geotextile protection layer
488 offers some benefit in reducing strains although the long-term survivability of the
489 geotextile needs to be seriously considered and the leakage is still very large.

490 For the GP subgrade at $\sigma_v = 500$ kPa, the calculated leakage ranges between
491 265,000 and 2,618,000 liters per hectare per day (lphd). When the stress is increased to
492 2000 kPa for the same GP subgrade, the leakage increases to between about 929,000
493 and 9,182,000 lphd. Again, the addition of the geotextile protection layer offers some

494 benefit in reducing strains although, again, the long-term survivability of the geotextile
495 needs to be seriously considered, the leakages are still large.

496 For the SP subgrade at $\sigma_v = 2000$ kPa the leakage increases to between about
497 348,000 and 3,443,000 lphd. This highlights the critical long-term impact of gravel in
498 the subgrade, without sufficient finer material, can have on long-term liner leakage. For
499 all of the subgrades except SM, both with and without the geotextile, contaminant
500 impact calculations would be required to assess the consequences of the magnitude of
501 the calculated leakage.

502 While there maybe time dependent increases in strain above those obtained in a
503 100-hour test, any strain exceeding 6% can be considered problematic to the long-term
504 performance of the geomembrane and needs to be avoided if long-term performance is
505 required. The two SM subgrades compacted at water contents of 11% (i.e., optimum
506 water content and compaction) and 20% (i.e., soft subgrade) were both satisfactory for
507 minimizing the tensile strains induced in the GMB. At some facilities some sandy
508 tailings can be used as subgrade for a geomembrane to contain more aggressive (e.g.,
509 pyritic) tailings. Where a suitable subgrade is not available or can not be obtained for
510 local quarries, use of sand tailing, or manufacture by sieving unsuitable local soils, the
511 unevenness of the surface can be improved by heavy compaction to minimize subgrade
512 surface irregularity arising from the surface unevenness due to protruding particles. If
513 heavy rolling is not sufficient, consideration may be given to placing a layer GTX above
514 the subgrade below the geomembrane to reduce strains. However there is a serious

515 question as to long-term performance of these geotextiles and hence they are not
516 recommended for this purpose, although they may be useful to minimize the risk of
517 piping of tailings in the shorter term. Since this is a temporary need for the GTX, a
518 suitable GTX, selected to have adequate filtration characteristics and service life, may
519 be appropriate. Two other potential solutions that may be combined with heavy rolling
520 the subgrade include (a) distributing a layer of soil with a maximum particle size of ~
521 2mm over the surface to sufficient thickness to prevent excessive strains, or (b) placing
522 a GCL with 4800 g/m² of dry bentonite between the subgrade and the geomembrane.
523 In both cases, tests should be conducted to confirm suitability of the proposed solution
524 at the expected applied stress.

525 **5. Summary and Conclusions**

526 Experiments were conducted to quantify the short-term tensile strains induced in a 1.5-
527 mm-thick HDPE geomembrane (GMB). Four subgrades, a poorly graded gravel (GP),
528 a well-graded gravel (GW), a poorly graded sand (SP), and silty sand (SM), and two
529 different nonwoven needle-punched geotextiles with mass per unit area of 450 g/m²
530 (GTX1) and 1420 g/m² (GTX2) were evaluated. The tensile strains were measured at
531 the applied vertical pressures of 500, 1000, and 2000 kPa for 100 h at a temperature of
532 21 ± 2 °C. For the specific conditions and materials examined, the following
533 conclusions were reached:

- 534 1) No puncture was observed.
- 535 2) The GP subgrade was the coarsest material and had ~ 460 tensile strains/m²

536 exceeding 6% and ~400 tensile strains/m² exceeding 12% at 2000 kPa. This has the
537 capacity to generate 4.6 million holes per hectare with time and leakages up to 9
538 million lphd that would require a contaminant impact assessment.

539 3) The GW subgrade had the same 76% coarse fraction (≥ 6.7 mm) as GP, but was
540 more well-graded and contained more sand size particles with a similar minimum
541 grain size as that for SP. At 2000 kPa, it generated ~ 390 tensile strains/m²
542 exceeding 6% that can be expected to generate 3.9 million holes per hectare with
543 time and leakages likely to be up to 7.8 million lphd.

544 4) The finer SP subgrade had same shaped gradation curve as GP, and this reduced the
545 number of tensile strains/m² exceeding 6% to about 174, but this could still generate
546 174,000 holes per hectare with time and leakages up to about 3.4 million lphd.

547 5) For the SM subgrade, the tensile strain no larger than 2% was observed at 2000 kPa.
548 Thus, the silty sand subgrade was very effective in reducing local indentations in
549 the GMB and providing a very long service life for an appropriately selected HDPE
550 geomembrane.

551 6) While both the 450 g/m² GTX1 and 1420 g/m² GTX2 protection reduced the
552 maximum tensile strain. However, the leakages were still relatively large (varying
553 from 46,000 lphd to 6,400,000 lphd) assuming strains exceeding 6% would result
554 in a stress crack without even considering the long-term survivability of the
555 geotextile. For both reasons, the use of the geotextile tested herein to mitigate the
556 unsatisfactory subgrade is unlikely to be a good long-term option for conditions

557 similar to those examined.

558 7) An appropriate HDPE or LLDPE geomembrane can be expected to perform very
559 well limiting leakage levels for an extremely long time (Rowe 2020), provided they
560 are well constructed on a suitable subgrade that does not generate significant (>5%)
561 tensile strain in the geomembrane.

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568 **Competing Interests**

569 The authors declare there are no competing interests.

570 **Data Availability Statement**

571 Data generated or analyzed during this study are provided in full within the published
572 article.

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714

Table 1. Geomembrane index tensile properties (measured following ASTM D6693

unless otherwise noted)

Property	Direction	Mean	Standard deviation
Yield strength (kN/m)	Machine	29	1
Break strength (kN/m)		47	2
Yield strain (%)		22	1
Break strain (%)		820	30
Yield strength (kN/m)	Cross-machine	31	0.5
Break strength (kN/m)		47	2
Yield strain (%)		18	0.5
Break strain (%)		870	50
Crystallinity (%) (ASTM E794)		52	0.5

Table 2. Properties of tailings and subgrade tested

Material	D_{10} (mm)	D_{30} (mm)	D_{60} (mm)	D_{85} (mm)	C_u	C_c
Tailings	0.02	0.07	0.19	0.4	9.8	1.4
GP subgrade	4.7	8.3	18.8	37.7	4.0	0.8
GW subgrade	2.1	8.3	18.8	37.7	8.8	1.7
SP subgrade	0.75	1.3	3.0	6.0	4.0	0.8
SM subgrade	0.03	0.12	0.23	0.4	6.5	1.7

Note: D_{10} , D_{30} , D_{60} , and D_{85} represent the diameter of grain size at which 10%, 30%, 60%, and 85% by mass is finer, respectively. C_u is the coefficient of uniformity. C_c is the coefficient of curvature.

Table 3. Index properties of examined nonwoven needle-punched geotextiles

Property	Method	Unit	GTX designation (mean \pm standard deviation)	
			GTX1	GTX2
Mass per unit area	ASTM D3776	g/m ²	450	1420
Thickness	ASTM D5199	mm	3.5	6.4
Tensile peak strength	ASTM D5035	N	805 \pm 40	1820 \pm 130
Elongation at peak tensile strength	ASTM D5035	mm	60 \pm 10	85 \pm 20
Tensile break strength	ASTM D5035	N	780 \pm 40	1440 \pm 90
Elongation at break tensile strength	ASTM D5035	mm	60 \pm 10	85 \pm 20
Puncture resistance	ASTM D4833	N	1660 \pm 320	2720 \pm 130
Tear strength	ASTM D4533	N	2340 \pm 110	3200 \pm 40
AOS	ASTM D4751	μ m	150	75

Table 4. Test conditions for GMB tensile strain and three largest strains for each test

Test No.	Underliner	Applied pressure σ_v (kPa)	No. of indentation scanned	No. of strain* $\geq 6\%$	Largest tensile strain (%)		
					<i>a</i>	<i>b</i>	<i>c</i>
1	GP	500	30	30 ^b	14	14	12
1A	GP+GTX1	500	23	6	7	6	6
2	GP	1000	25	24	17	16	14
2A	GP+GTX1	1000	28	20	10	9	9
3	GP	2000	40	40 ^b	32	29	25
3R ^e	GP	2000	58	58 ^e	30	27	26
3A	GP+GTX1	2000	29	28	23	22	19
3B	GP+GTX2	2000	24	11	14	12	11
4	GW	500	23	9	9	8	8
5	GW	1000	20	14	14	12	10
6	GW	2000	36	34	16	15	15
6A	GW+GTX1	2000	19	12	8	8	7
7	SP	2000	24	15	13	11	9
7A	SP+GTX1	2000	13	2	6	6	5
8	SM ^c	500	1	0	2	N/A ^a	N/A ^a
9	SM ^d	2000	1	0	N/A ^a	N/A ^a	N/A ^a

Note: * In an area of 0.0864 m². ^aNo discernable indentation. ^bThe minimum scanned strain was 6%. ^cThe underliner was compacted at ~20 % gravimetric water content (the Standard Proctor optimum moisture content was 11%). ^dThe underliner was compacted at the Standard Proctor optimum moisture content of ~11%. ^eRepeat test, the minimum scanned strain for those 58 indentations analyzed was 7%.

Table 5. Expected leakage for stress cracks of three assumed sizes

σ_v (kPa)	Subgrade	Strains $\geq 6\%$		$L = 10$ mm $B = 0.5$ mm	$L = 20$ mm $B = 1.6$ mm	$L = 30$ mm $B = 1.75$ mm
		(#/m ²)	(#/ha)	Q (lphd)	Q (lphd)	Q (lphd)
500	GP	347	3,470,000	265,000	1,133,000	2,618,000
500	GP+GTX1	69	694,000	53,000	227,000	524,000
500	GW	104	1,040,000	79,000	340,000	785,000
500	SM	0	0	-	-	-
1000	GP	289	2,890,000	367,000	1,568,000	3,625,000
1000	GP+GTX1	231	2,310,000	293,000	1,255,000	2,900,000
1000	GW	162	1,620,000	205,000	878,000	2,030,000
2000	GP	463	4,630,000	929,000	3,973,000	9,182,000
2000	GP+GTX1	324	3,240,000	650,000	2,781,000	6,427,000
2000	GP+GTX2	127	1,270,000	255,000	1,093,000	2,525,000
2000	GW	394	3,940,000	790,000	3,377,000	7,804,000
2000	GW+GTX1	139	1,390,000	279,000	1,192,000	2,754,000
2000	SP	174	1,770,000	348,000	1,490,000	3,443,000
2000	SP+GTX1	23	230,000	46,000	199,000	459,000
2000	SM	0	0	-	-	-

$t = 1.5$ mm, $k_2/k_1 = 1.17$, $k_1 = 1.5 \times 10^{-8}$ m/s at $\sigma_v = 500$ kPa, $T = 25$ m, $H = 26$ m; $k_1 = 1.2 \times 10^{-8}$ m/s at $\sigma_v = 1,000$ kPa, $T = 50$ m, $H = 54$ m; $k_1 = 0.95 \times 10^{-8}$ m/s at $\sigma_v = 2,000$ kPa, $T = 100$ m, $H = 108$ m (Note: t is GMB thickness, k_1 is hydraulic conductivity within the GMB defect and predicted based on the empirical relationship by Rowe and Fan (2022), k_2 is the hydraulic conductivity for tailings directly above the defect, T is the tailings thickness, H is the water head above the GMB, L is the equivalent rectangular length of the stress crack, B is the equivalent rectangular width of the stress crack, Q is the predicted leakage based on the method summarized by Rowe and Fan (2022))

Figure Captions

Fig. 1. Cross section through a typical test cell used in experiments (modified from Fan and Rowe 2022b)

Fig. 2. Grain size distributions of silty sand tailings and four subgrade materials

Fig. 3. Particle shapes from subgrades: (a) GP; (b) GW; (c) SP

Fig. 4. Photographs showing a 160 mm × 270 mm region of the lead sheet in Test 9 with SM subgrade compacted at the Standard Proctor optimum moisture content for: (a) before the experiment, and (b) after applying the 2000 kPa consolidation stress for over 100 hours

Fig. 5. Seven largest strains calculated from each test showing the effect of subgrade for: (a) Tests 1 and 4 at 500 kPa, (b) Tests 2 and 5 at 1000 kPa, and (c) Tests 3, 6 and 7 at 2000 kPa

Fig. 6. a) Illustration of coarse gravel (GP) contact leading to higher local indentations in a GMB. b) Illustration of the impact of finer component in reducing local indentations in a GMB. c) Illustration of the impact of GTX protection layer between coarse gravel and GMB in reducing local indentations.

Fig. 7. Effectiveness of geotextile (GTX) protection layer between the GMB and subgrade on reducing tensile strain at 2000 kPa for: (a) Tests 3, 3A and 3B, (b) Tests 6 and 6A, and (c) Tests 7 and 7A

Fig. 8. Three largest strains calculated from each test showing the effect of pressure, subgrade, and GTX protection layer

Fig. 9. Distributions of GMB tensile strains $\geq 5\%$ per square meter GMB with subgrades of GP, GW, and SP at 2000 kPa

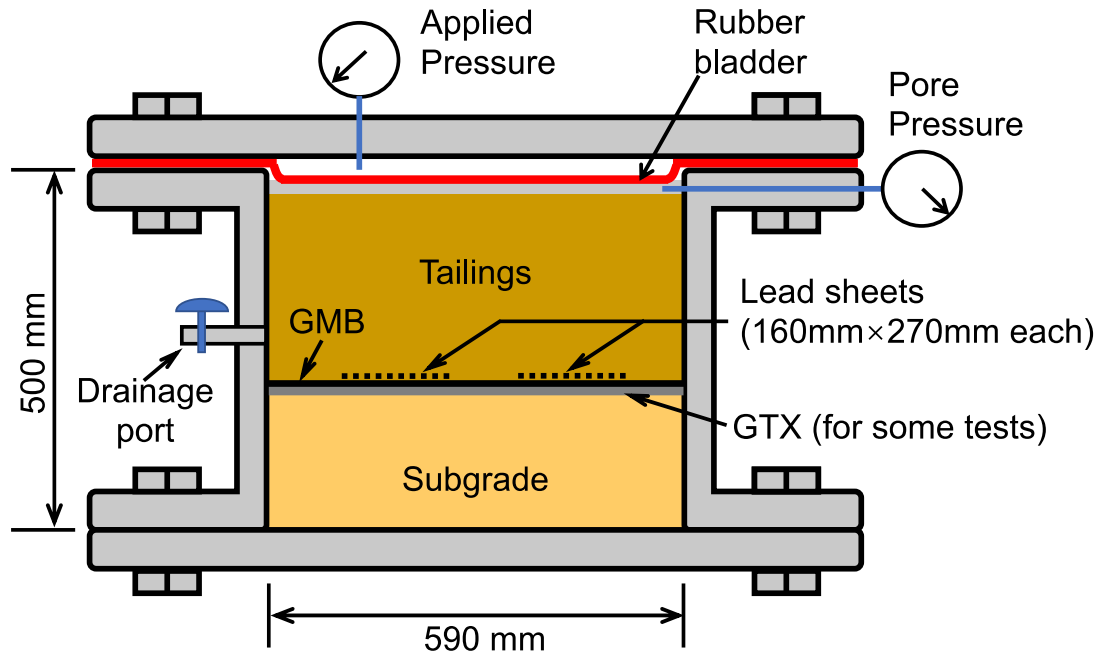


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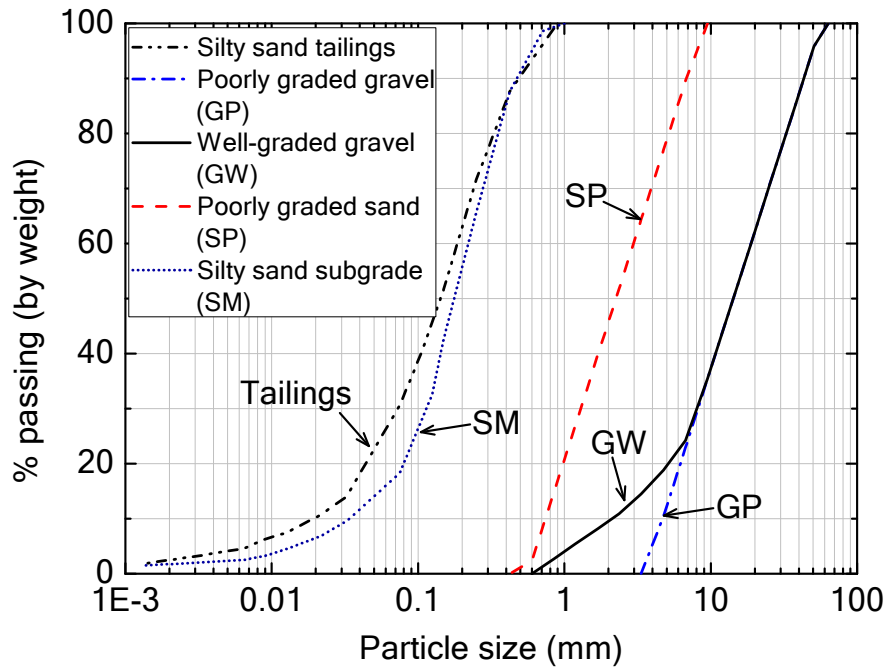


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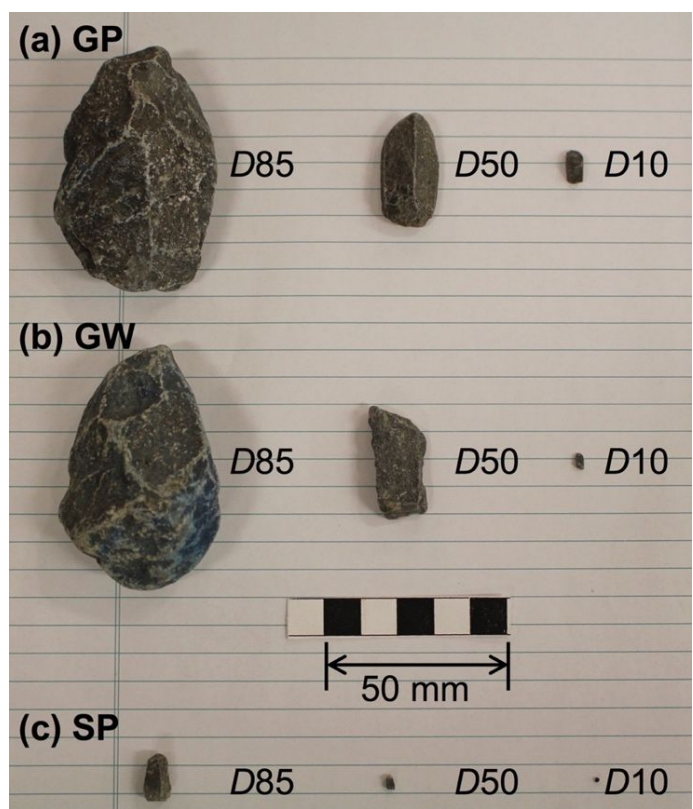


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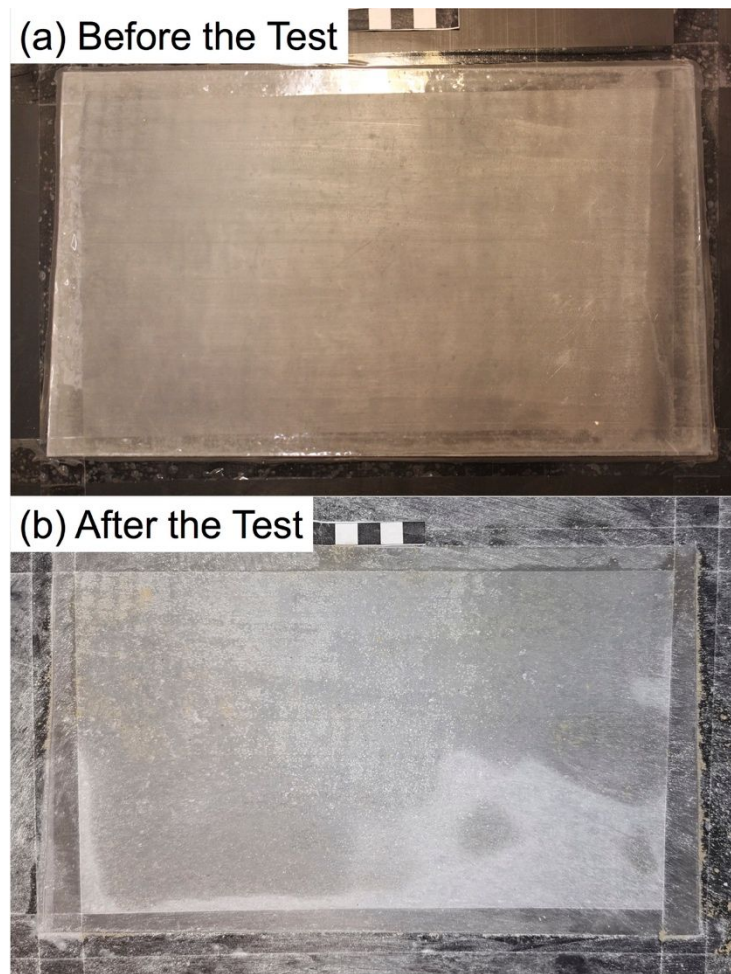
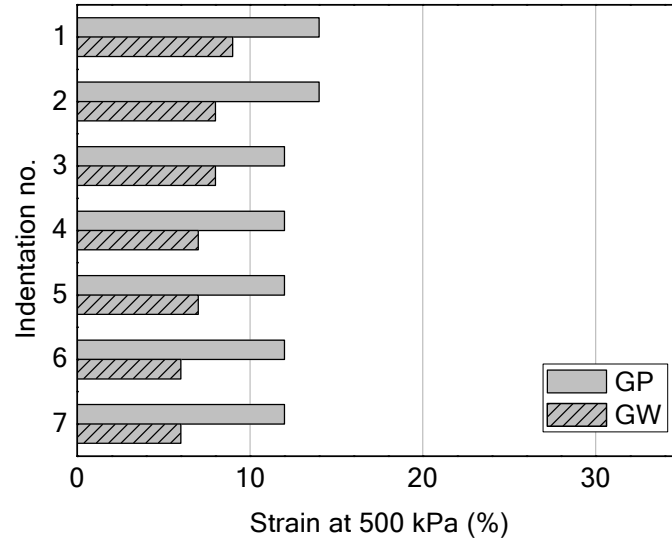
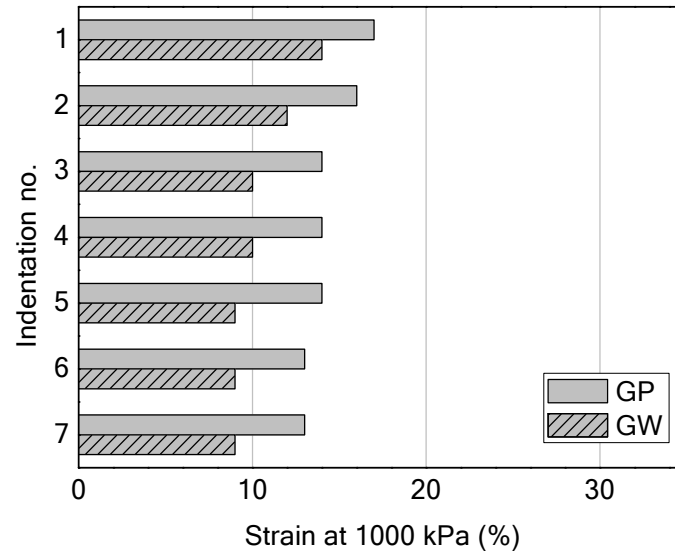


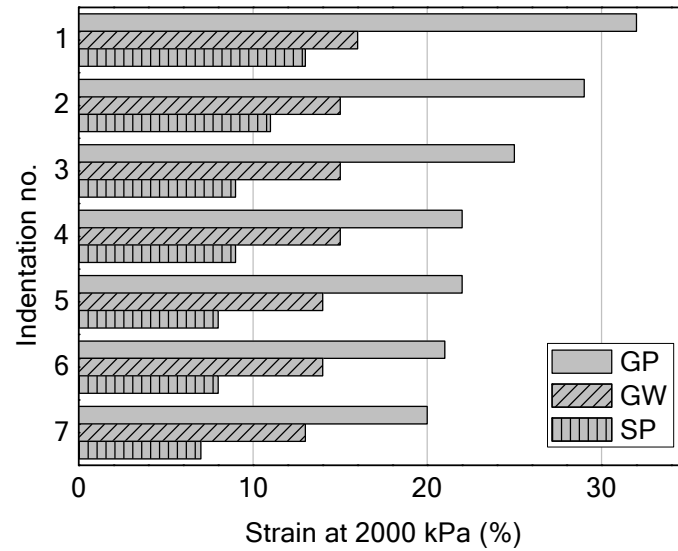
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(a) Tests 1 and 4



(b) Tests 2 and 5



(c) Tests 3, 6 and 7

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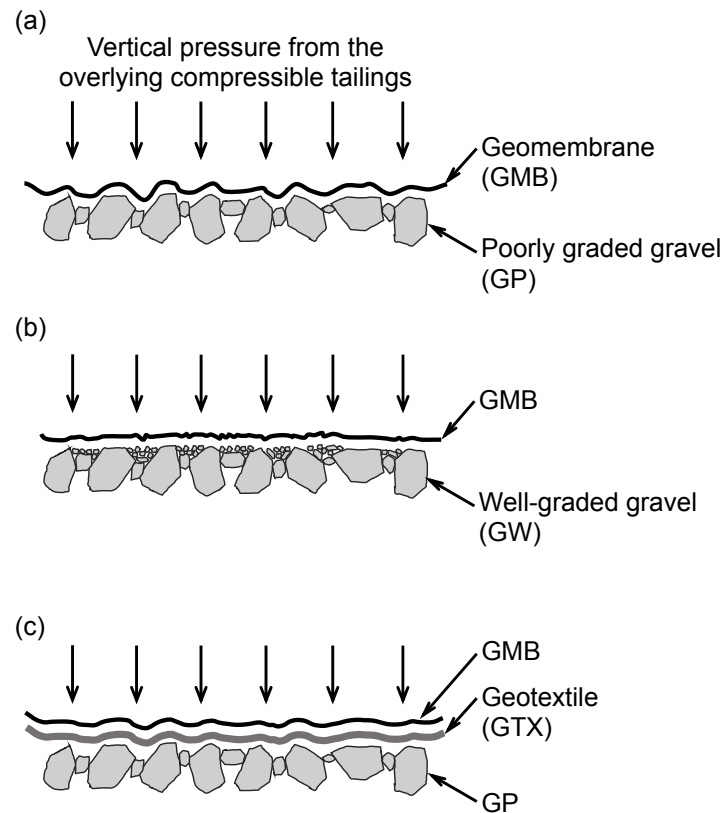
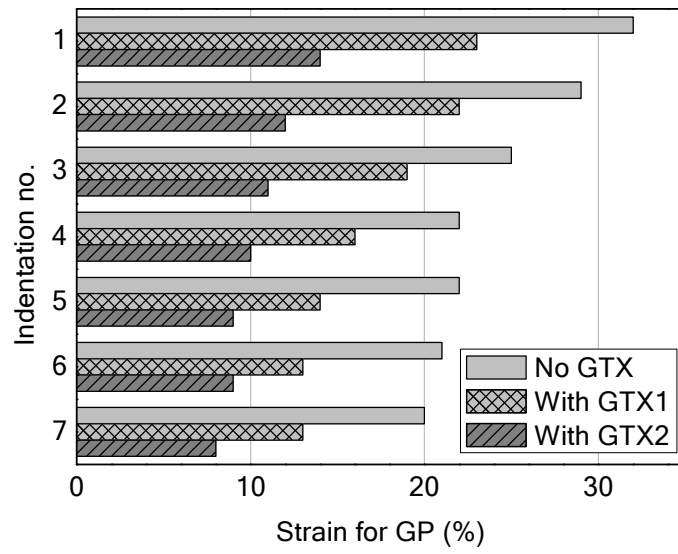
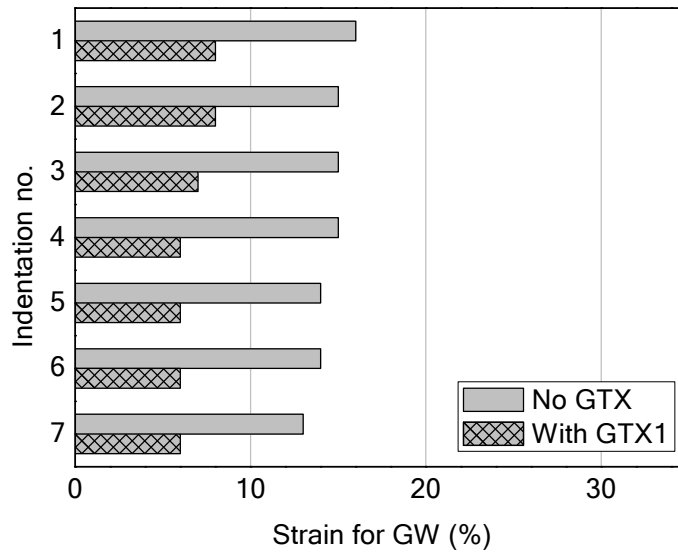


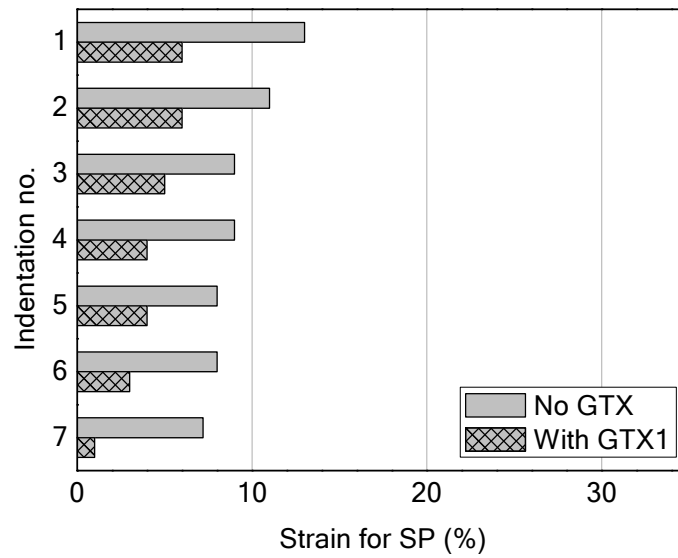
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(b) Tests 6 and 6A



(c) Tests 7 and 7A

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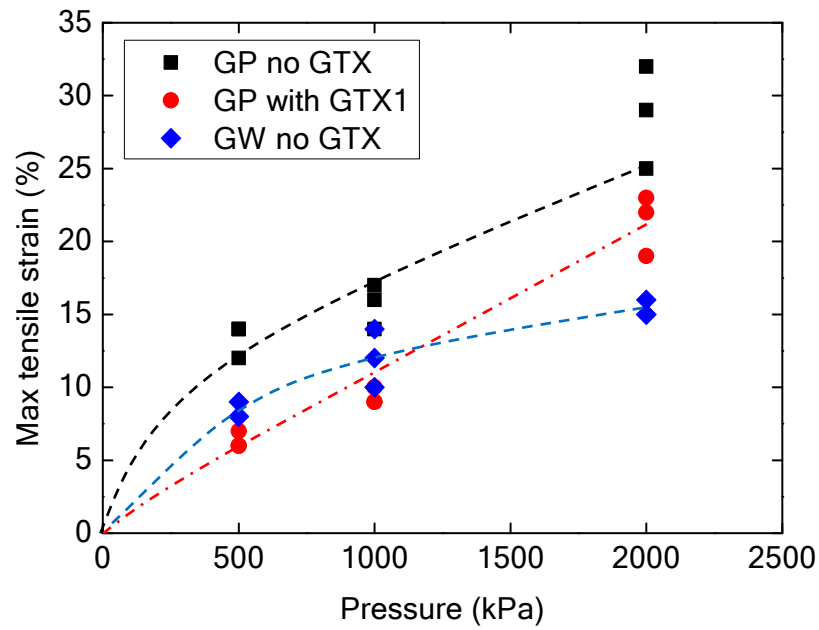


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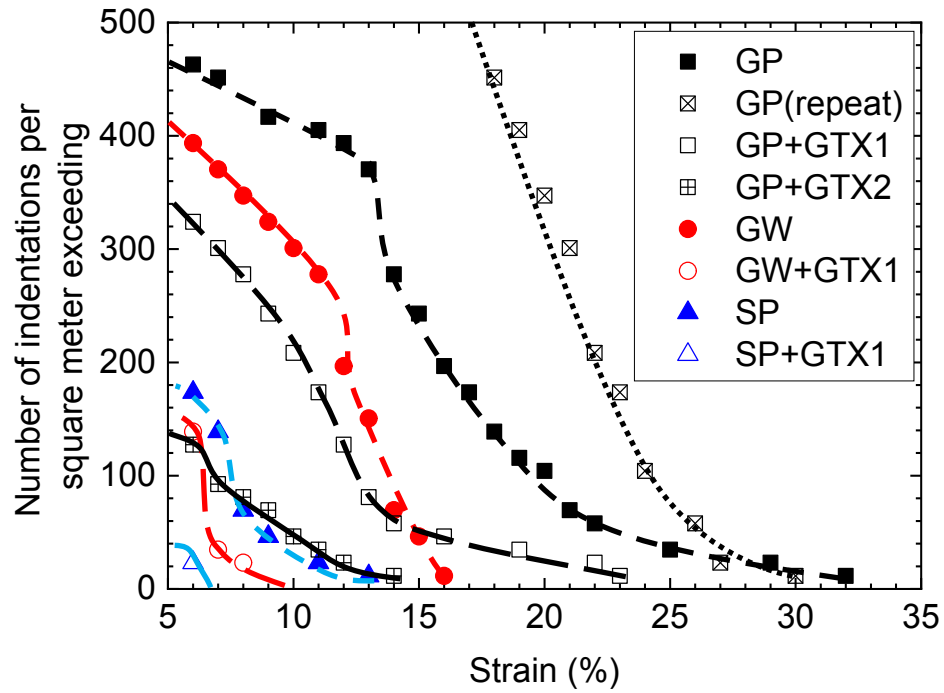


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